



## Effect or Treatment Heterogeneity?

### Policy Evaluation with Aggregated and Disaggregated Treatments

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# Motivation

Researchers and practitioners in business, economics, medicine and beyond are often interested in heterogeneous effects of ads/policies/treatments/...

⇒ Who benefits or loses by how much ⇒ personalized ads, policy, medicine, ...

⇒ Much is known about **how** to estimate heterogeneous effects

- Classic subgroup analysis or interaction terms (standard)
- A-/DR-/R-/S-/T-/X-/...-learner or Causal BART/Boosting/Forest/Tree/... (new)

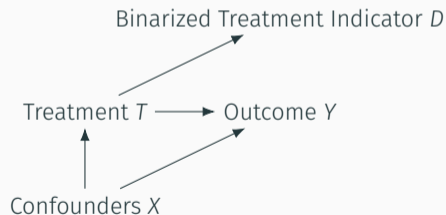
Less work on the conceptual side: **What** do we estimate?

This paper focuses on the common case where an evaluated binary treatment can be conceived as being itself heterogeneous

## Scenario 1: binarized treatment

Multi-valued treatments are aggregated into a binary indicator

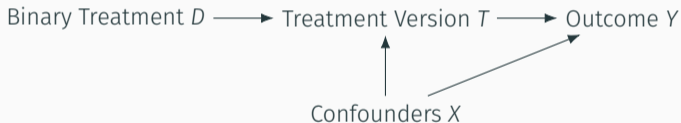
- different smoking intensities subsumed in "smoking yes/no"
- pollution intensity binarized into "pollution high/low"



## Scenario 2: Multiple treatment versions

Binary treatment can be disaggregated in taking multiple versions

- marketing measures or surgeries delivered by different people
- different specializations within job training program



RQ: What do heterogeneous effects mean if the treatment is heterogeneous?  
And what can we do about it?

## Illustrating toy example - average effect

Evaluation of marketing measure to increase customer satisfaction using a randomized controlled trial (A/B testing)

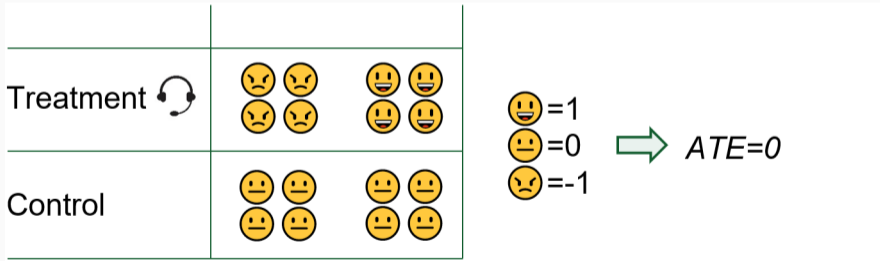
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# Illustrating toy example - average effect

Evaluation of marketing measure to increase customer satisfaction using a randomized controlled trial (A/B testing)

The measure is to call customers and to inform about new exciting products

First check the AVERAGE TREATMENT EFFECT (ATE)



## Illustrating toy example - heterogeneous effects





The goal of **canonical effect heterogeneity** analysis is to figure out whether at least **some groups respond positively** to treatment




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	♀	♂
Treatment 🎧		
Control		

 = 1  
 = 0  
 = -1





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 $CATE(\text{♂}) = 1$






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⇒ Only men should be treated

Causal Machine Learning does this personalization nowadays in a data-driven way

## Illustrating toy example - treatment heterogeneity

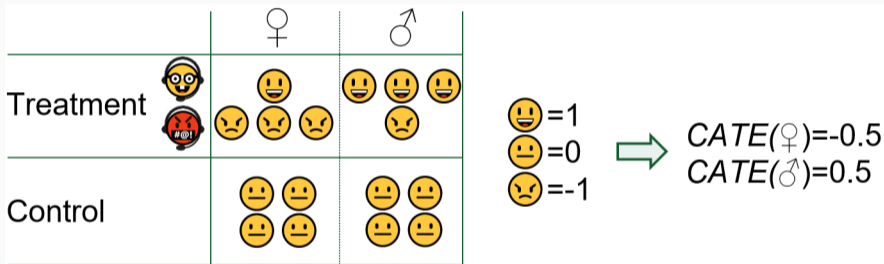
It is **unlikely** that all customers receive the **same (homogeneous) treatment**

Example: Different employees deliver the call, but not random across groups

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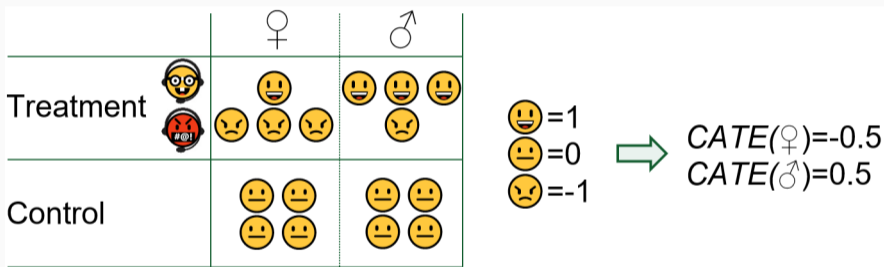
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## Illustrating toy example - treatment heterogeneity

It is **unlikely** that all customers receive the **same (homogeneous) treatment**

Example: Different employees deliver the call, but not random across groups



“Effect heterogeneity” is driven by **different groups receiving different treatments**

NOT that different groups respond differently to the same treatment

# Consequences

The **standard conclusion** would be to **target male customers**

However, this **ignores the mechanism** behind the heterogeneity

The **correct conclusion** would be that **women receive a worse treatment mix** and this should be fixed

We propose a **decomposition to disentangle effect and treatment heterogeneity**

## Illustrating toy example - decomposition



















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We call this benchmark parameter the RANDOMIZED CATE (*rATE*)

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→  $rATE(♀) = 0$   
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Treatment		 	 
		 	 
Control		 	 
		 	 

 = 1  
 = 0  
 = -1

➔  $rATE(♀) = 0$   
 $rATE(♂) = 0$

⇒ Gender gap in effectiveness disappears under same treatment composition

⇒ It was completely driven by treatment heterogeneity



## Illustrating toy example - decomposition

Difference between canonical *CATE* and *rATE* shows how much of the canonical *CATE* is driven by treatment heterogeneity:

- $\Delta(\varphi) = CATE(\varphi) - rATE(\varphi) = -0.5$
- $\Delta(\sigma) = CATE(\sigma) - rATE(\sigma) = 0.5$

Positive values indicate that the **assignment of treatment versions is better than random**

**Heterogeneity in  $\Delta(x)$**  indicates that the **selection quality of versions varies** across different groups

This can be used e.g. to understand the **fairness** of the current assignment mechanism of treatment versions

## Application: Job Corps

Job Corps is the largest training program for disadvantaged youth (16–24) in the US

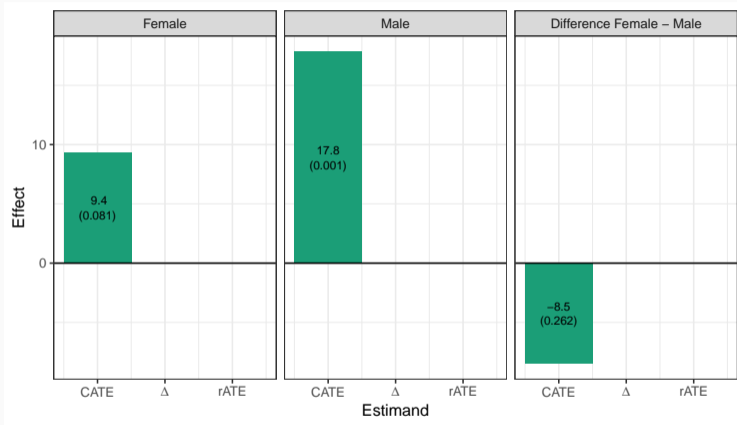
Experimental assessment from 1994–1996 (Schochet et al., 2001, 2008)

**Common finding:** women profit less in terms of earnings than men

**Potential explanation:** Vocational training of men in JC focuses more on craft jobs, for women more on service oriented  $\Rightarrow$  Lower returns to vocational training

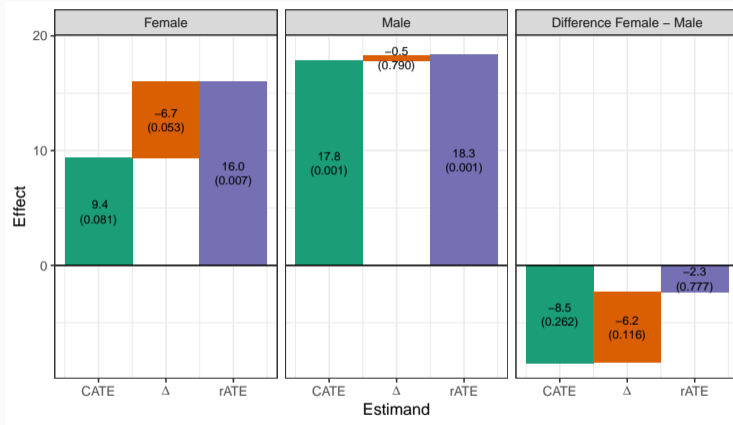
**Outcome:** weekly earnings four years after program start

# Application: Job Corps



Increase in women's earnings half of men's

# Application: Job Corps



Imposing the same vocational training nearly removes the gender gap

⇒ Targeting of vocational training for women worse than random

Interpretation of seemingly easy heterogeneous effects might be more complicated if analyzed treatment is itself heterogeneous

Our method provides a first way to address this issue

More in the paper:

- Double ML based estimator allowing for small p-scores and many treatments
- Application on ethnicity and age gaps in the effect of smoking on birthweight
- We provide an R implementation of the method (*causalDML*) and replication notebooks

**Thank you for your attention!**

paper on arXiv:2110.01427

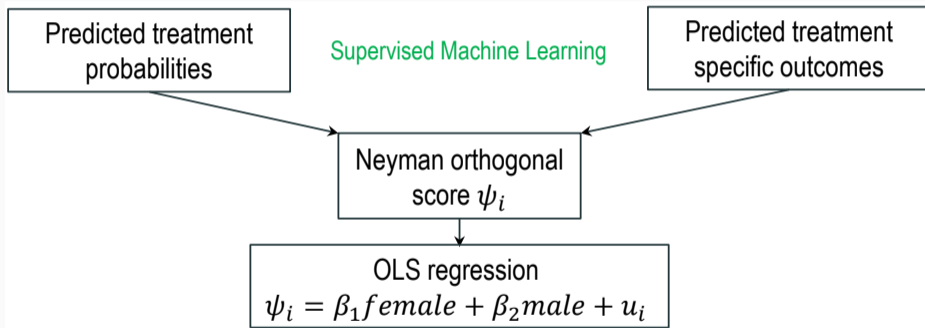
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# How does the estimation procedure work?

Double Machine Learning based estimator building on Semenova & Chernozhukov (2021):



$\psi_i$  is unbiased signal of decomposition parameters  $\Rightarrow$  pseudo-outcome

► formal